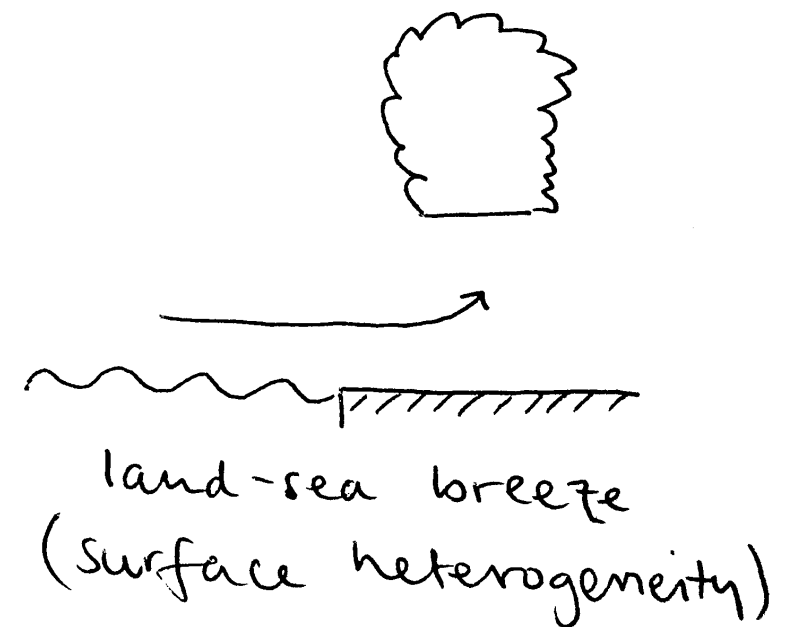
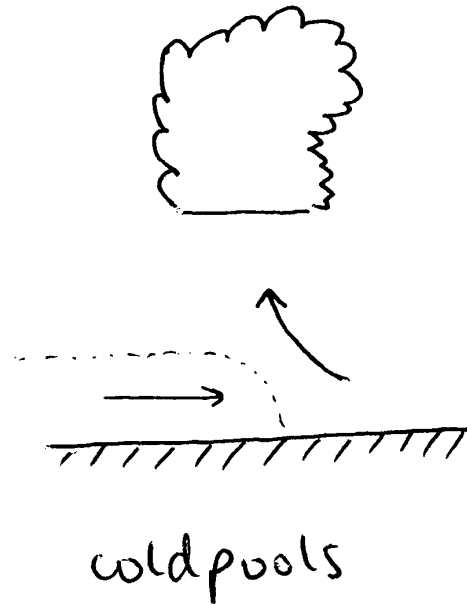
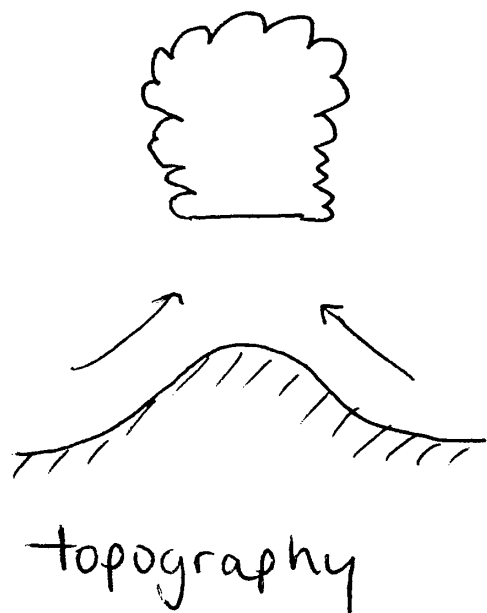


Aim

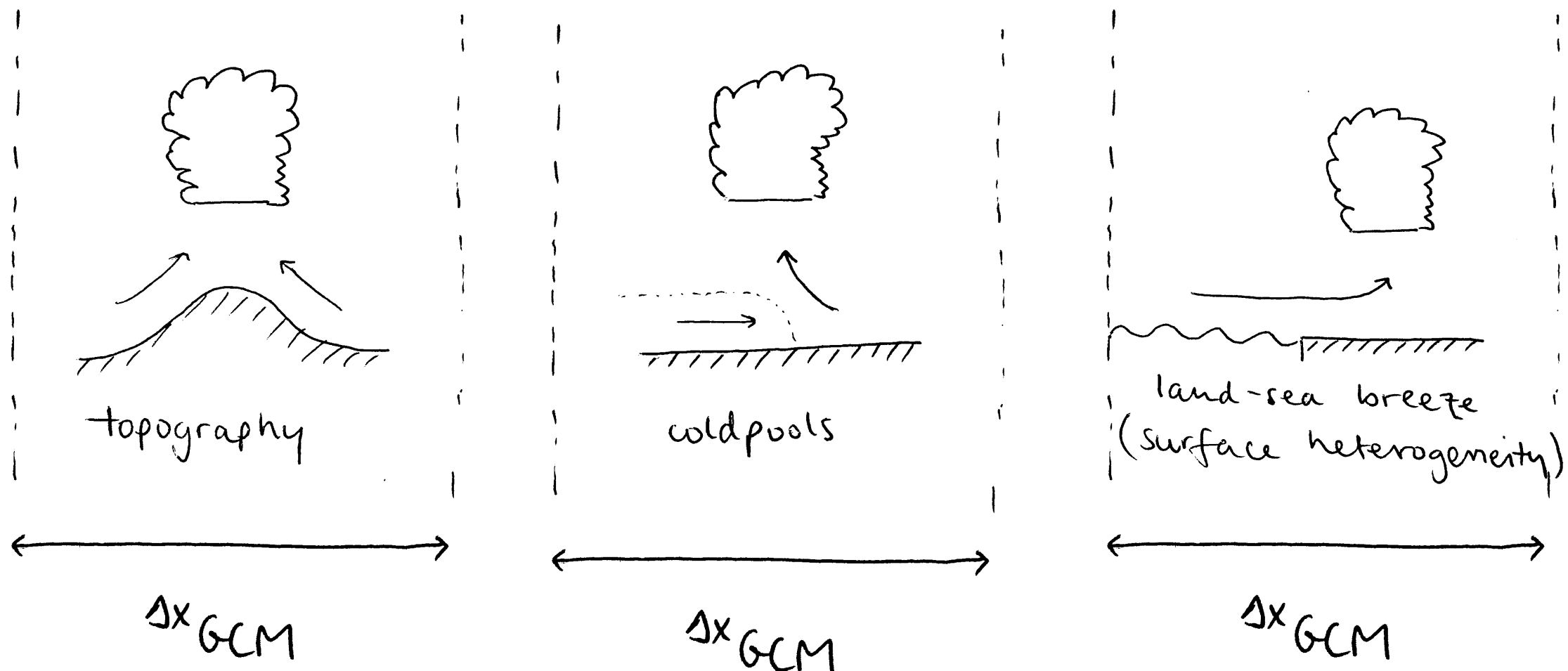
- Describe statistics of boundary layer relevant to triggering convection and the sensitivity to presence of different phenomena



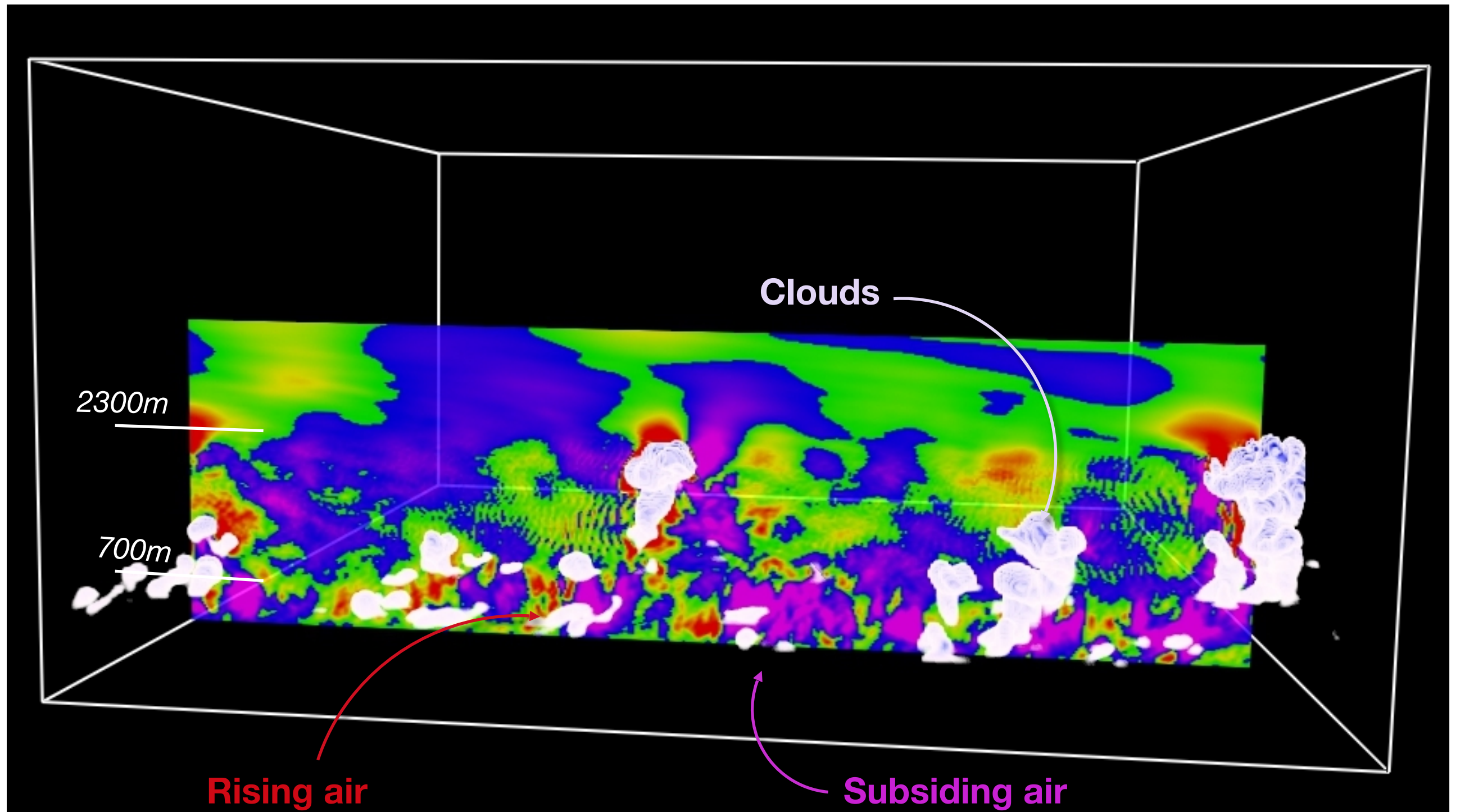
- *“What are the length-scales and magnitudes of perturbations which trigger convection?”*

Why?

- GCMs have too coarse resolution to fully represent convection ($O(\text{km})$)
 - ➔ Trigger (and evolution) of convection must be parameterised
 - ➔ These *sub-grid* features are known to be critical in predicting formation of convection



What are the length-scales of variability?

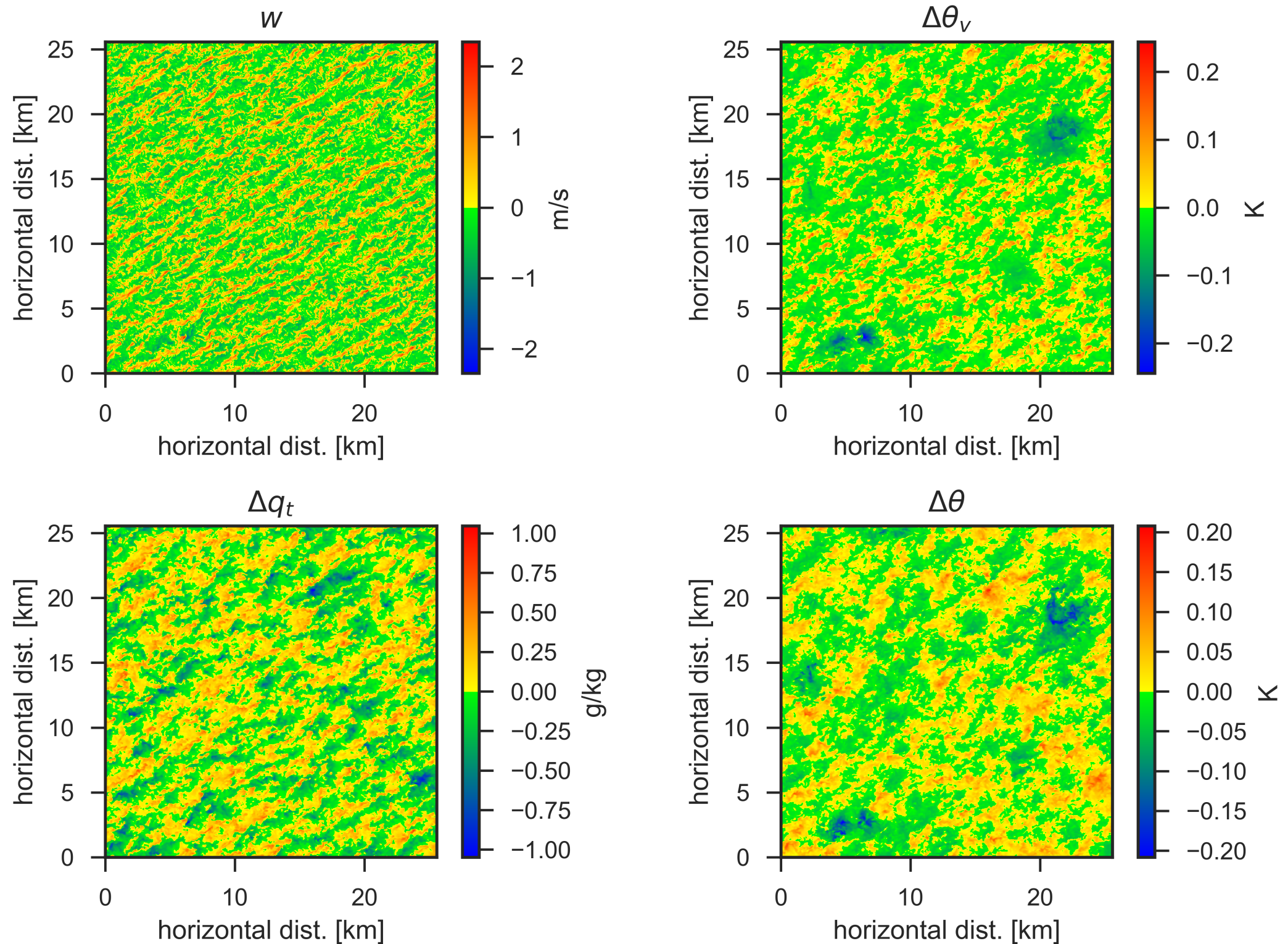


$\Delta x=25m$ Large-Eddy Simulation, RICO test-case

Rendered with VAPOR

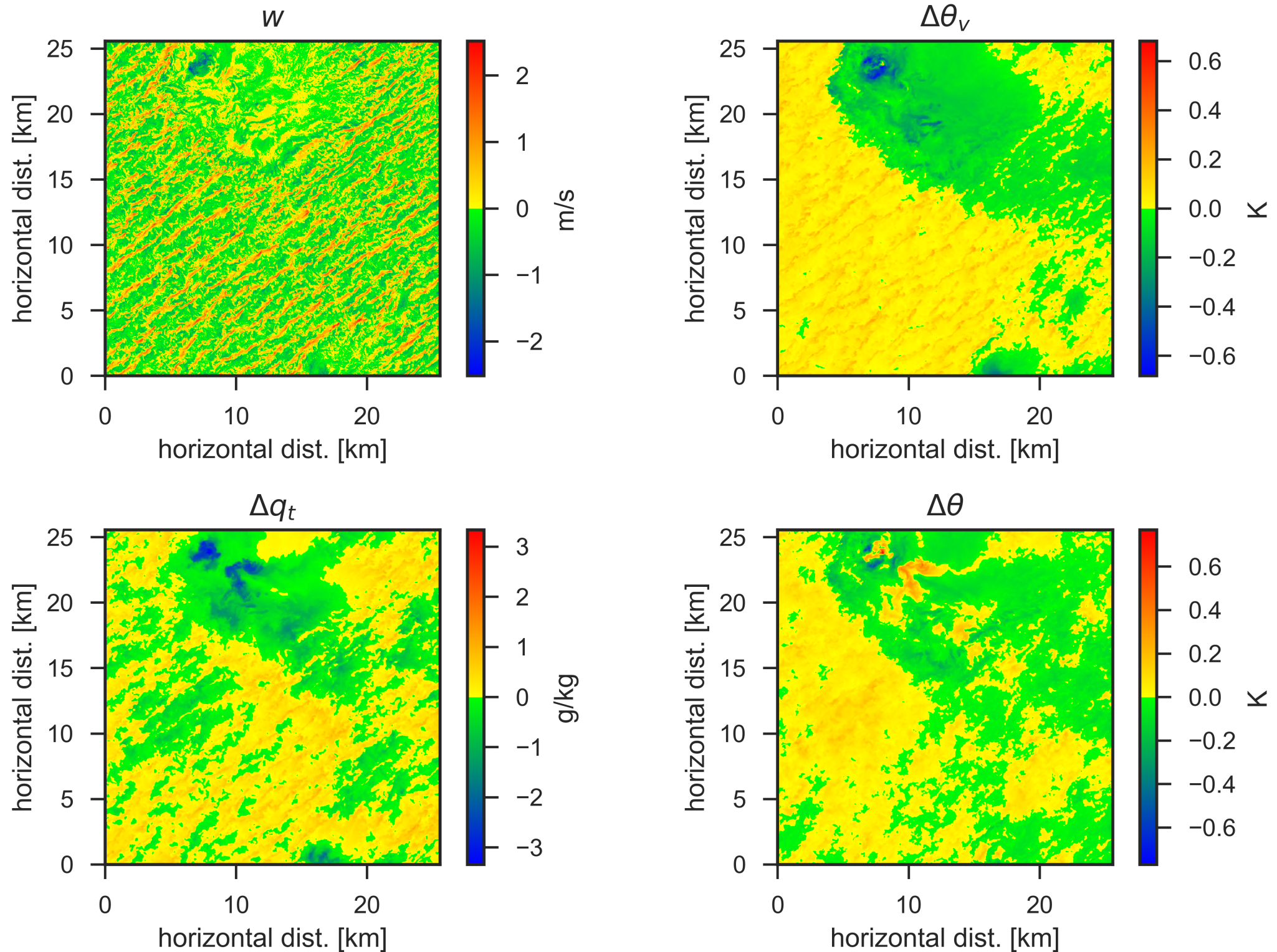
What are the length-scales of variability?

Cross-sections of scalar fields in RICO at $z=200.0\text{m}$ $t=480\text{min}$

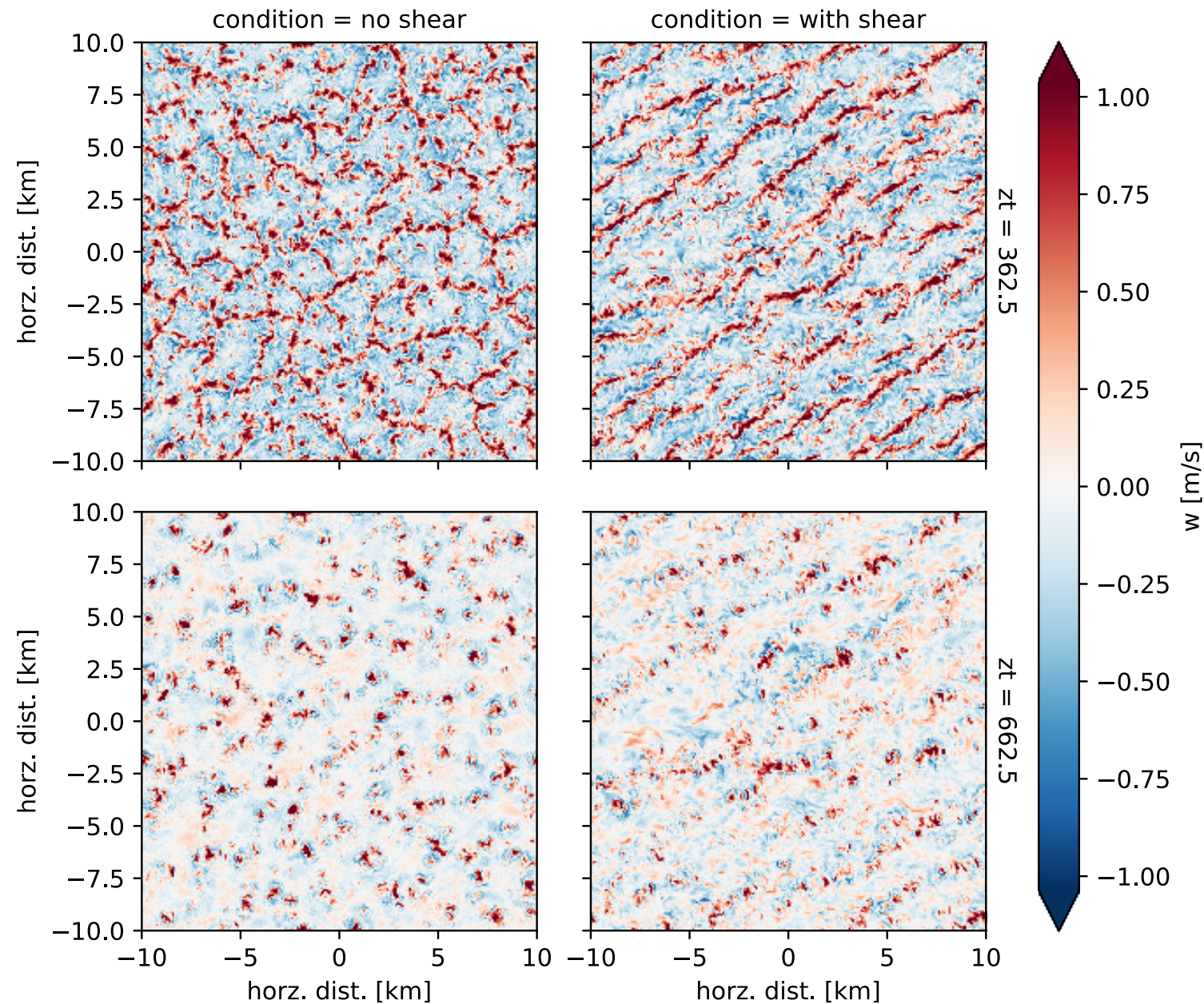


What are the length-scales of variability?

Cross-sections of scalar fields in RICO at $z=200.0\text{m}$ $t=1440\text{min}$

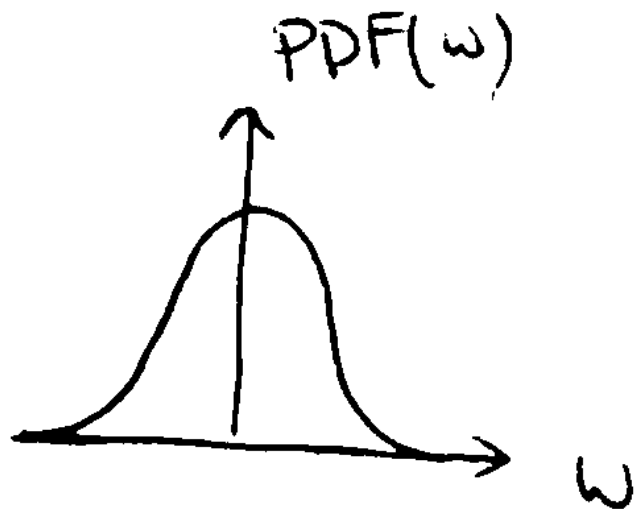


Example: shear/no-shear RICO-like simulations



- Fixed fluxes ($F_s=150\text{W}/\text{m}^2$, $F_l=7.0\text{W}/\text{m}^2$)
- Convective cells instead of rolls in boundary layer with shear
- In shear convection appears at ends of rolls?
- Without shear at nodes of cells?

Researching things relevant to convective parameterisation

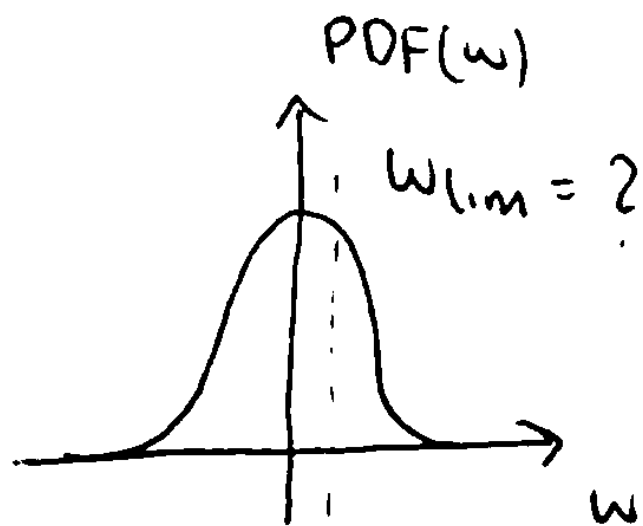


Hierarchy of analysis:

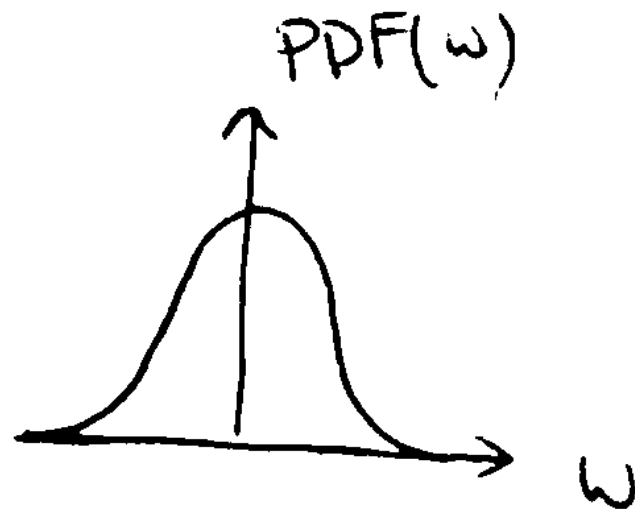
a) Vertical profiles of horizontally integrated properties, e.g. PDFs of scalars (without identifying triggering updrafts)

b) Vertical profiles of identified updraft regions (e.g. *two-fluid* partitioning)

- Is there an optimal partitioning of fluid between updrafts/environment?
- Interested in total BL vertical transport or only thermals which trigger convection?



Researching things relevant to convective parameterisation



Hierarchy of analysis:

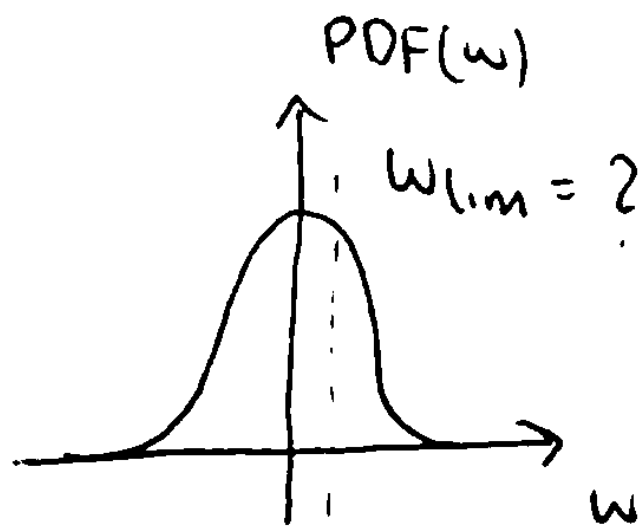
a) Vertical profiles of horizontally integrated properties, e.g. PDFs of scalars (without identifying triggering updrafts)

tools ready!

b) Vertical profiles of identified updraft regions (e.g. *two-fluid* partitioning)

- Is there an optimal partitioning of fluid between updrafts/environment?
- Interested in total BL vertical transport or only thermals which trigger convection?

I think so



Found method to identify these

Researching things relevant to convective parameterisation

Hierarchy of analysis:

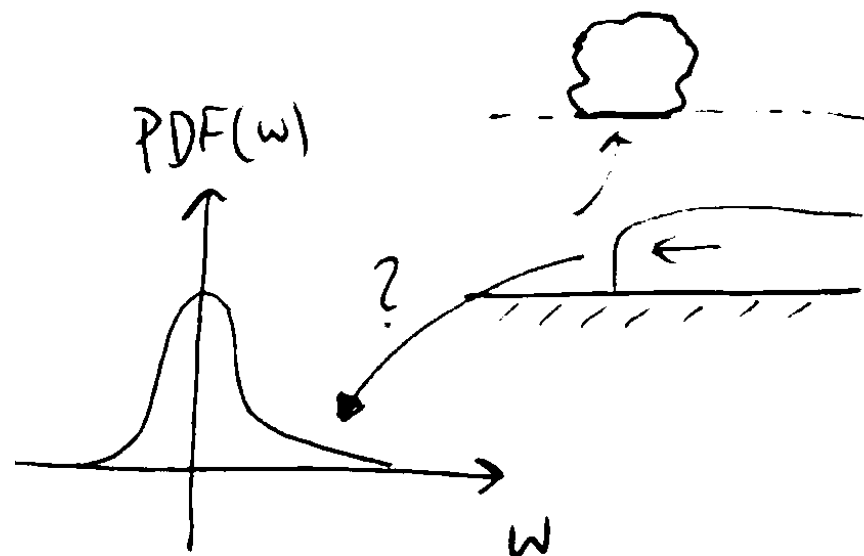
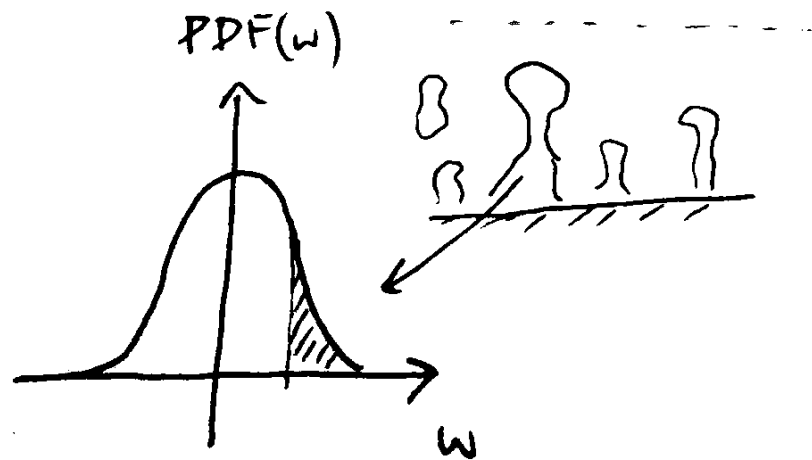
...

c) Object-based decomposition of horizontal variability

- e.g. reconstruct PDFs using only N -largest objects, construct *object size vs scalar perturbation* PDFs or identify triggering objects

d) Identify cause of change in vertical profiles and new scalar quantities which parameterise change

- e.g. *the presence of a cold pool with magnitude $\Delta\theta_v$ modifies the skewness of the $PDF(w)$ by $\alpha\Delta\theta_v$*



Researching things relevant to convective parameterisation

Hierarchy of analysis:

...

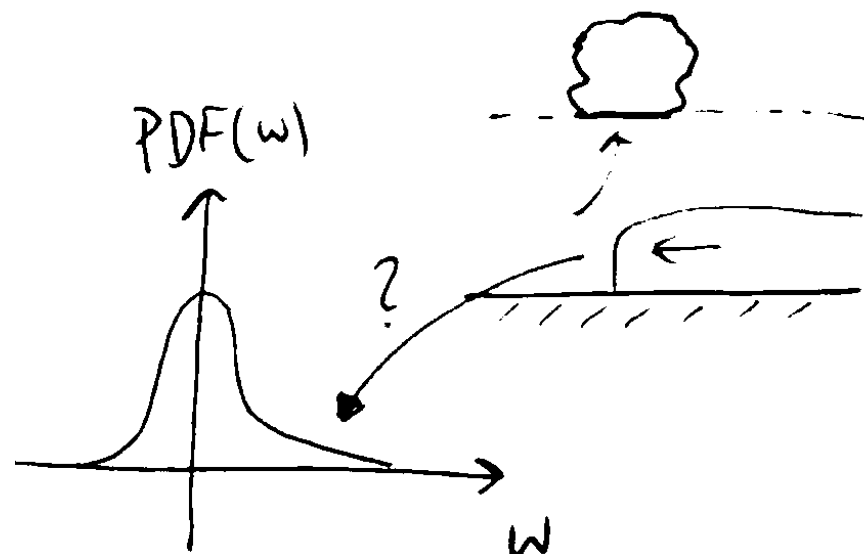
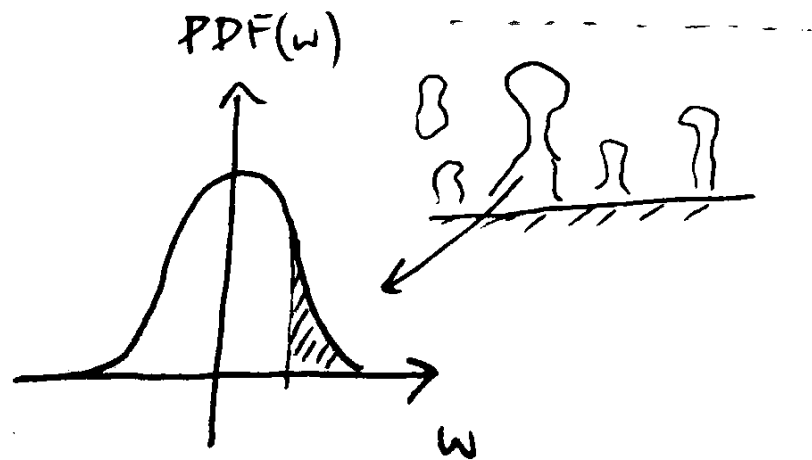
c) Object-based decomposition of horizontal variability

- e.g. reconstruct PDFs using only N -largest objects, construct *object size vs scalar perturbation* PDFs or identify triggering objects

some interesting results!

d) Identify cause of change in vertical profiles and new scalar quantities which parameterise change

- e.g. *the presence of a cold pool with magnitude $\Delta\theta_v$ modifies the skewness of the $PDF(w)$ by $\alpha\Delta\theta_v$*



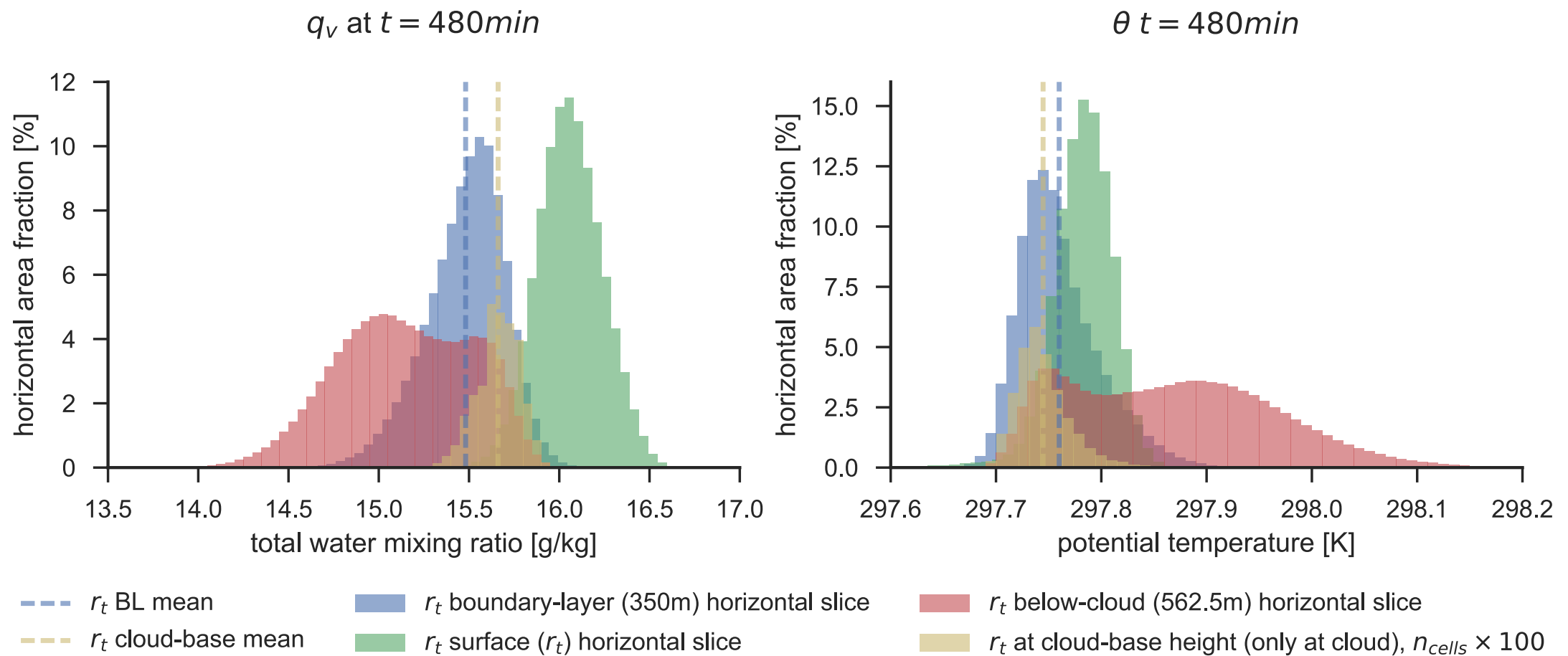
Ongoing



2 topics today

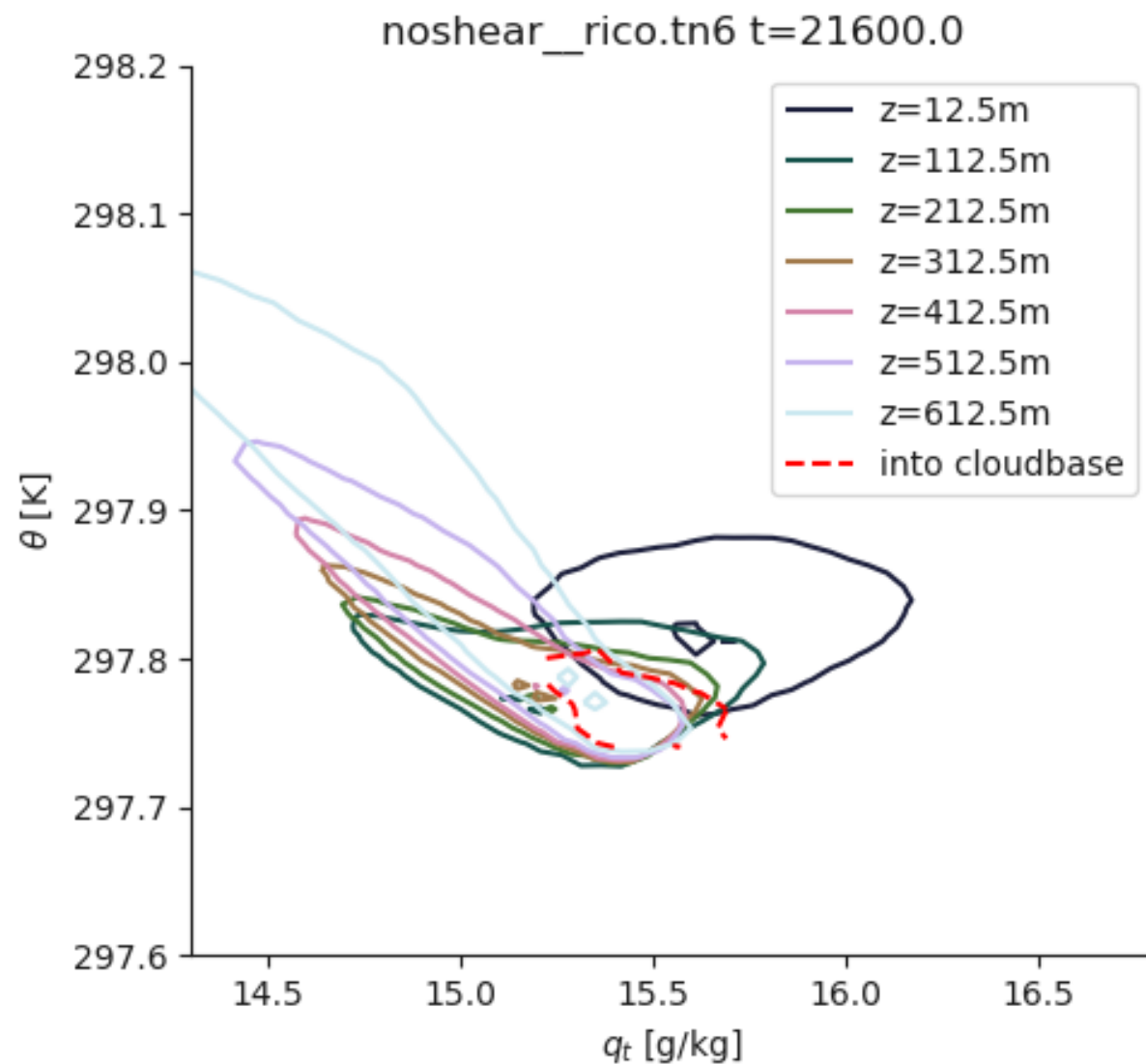
1. Statistical properties of *bulk* boundary layer and cloud-feeding air
 - i. Joint-distributions and characteristic length-scales in boundary-layer
2. Statistical properties of *individual* boundary-layer objects

1. Distributions of moisture and temperature (at interesting heights)



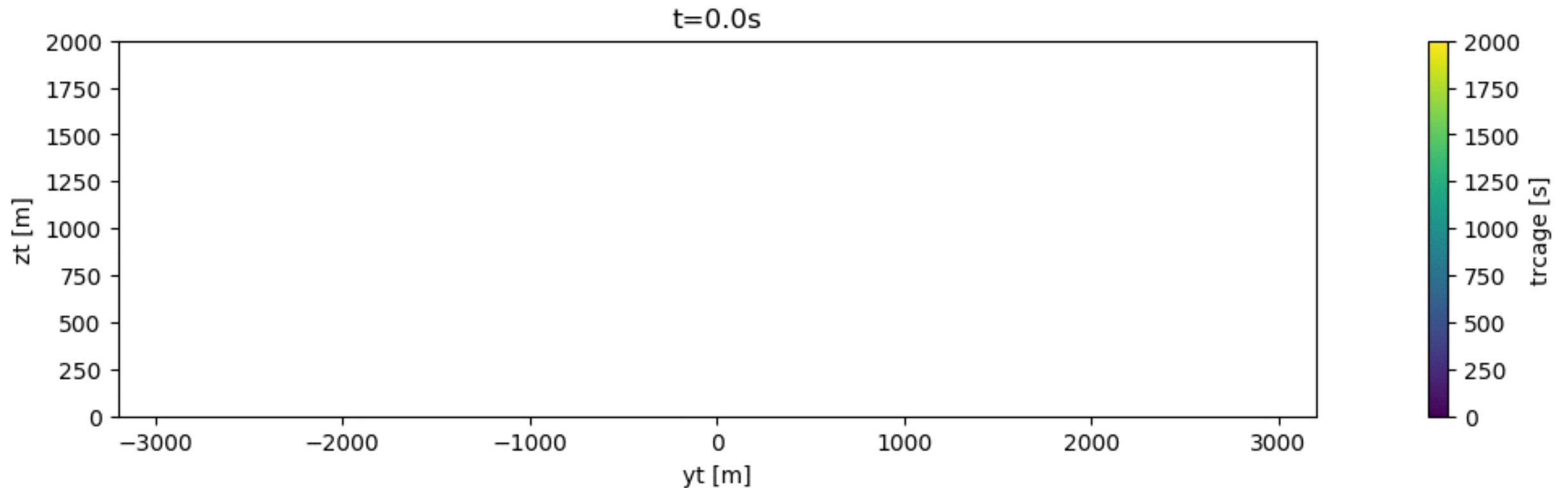
- Air that reaches cloud-level appears to be moister and colder than boundary layer characteristic values
- But *what are the joint distributions (and their height variation)?*

How does water vapour and temperature correlate in the boundary layer?



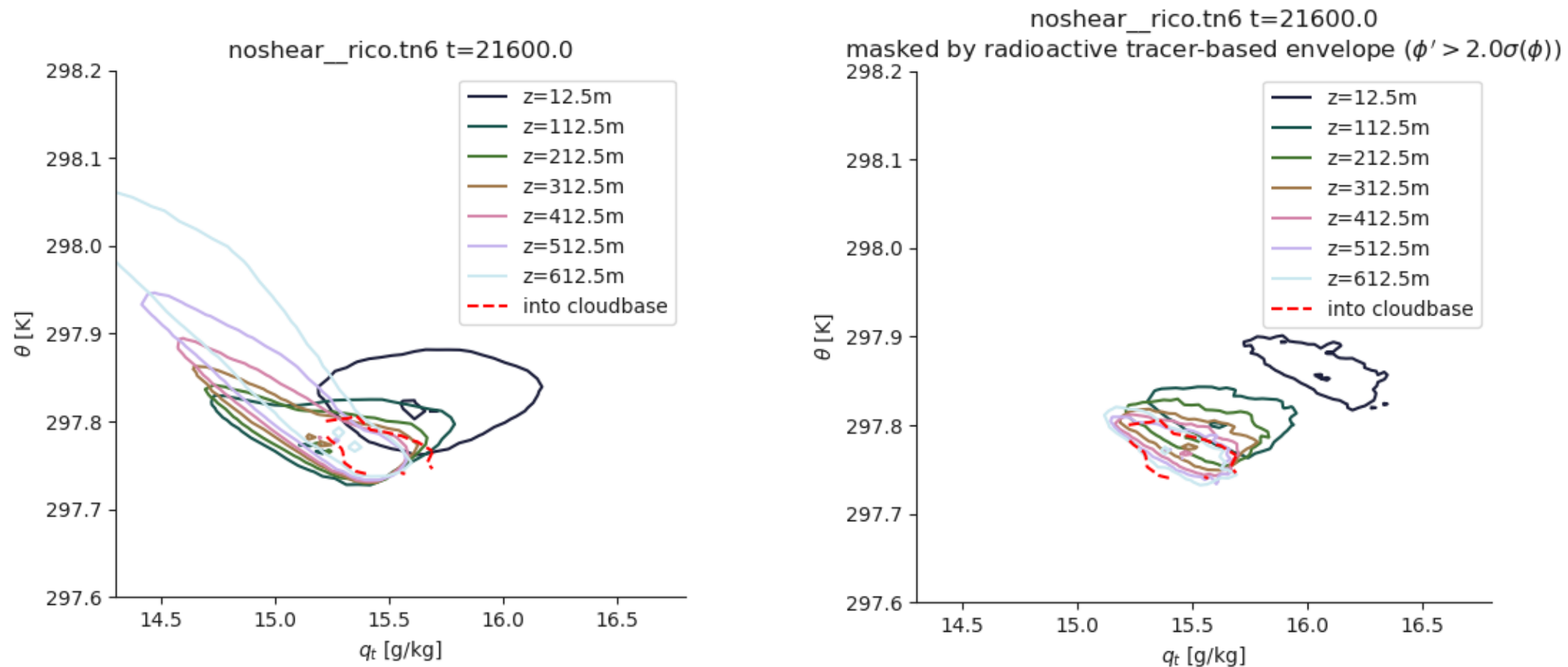
- Inner and outer contour at each height contain regions with top 5% and top 90% concentration of points respectively (“garlic plot”)
- Red contour: air Δx below tracked clouds within 3min of appearance => air entering clouds
- How can we *isolate the air that enters clouds*?

Boundary layer thermals marked with radioactive tracer



- Two tracers (ϕ_1, ϕ_2) with different half-life ($\tau_1=10\text{min}$, $\tau_2=15\text{min}$) released from surface
- Time since release: $t_{\text{age}} = \tau_1 \tau_2 \log(\phi_1 / \phi_2) / (\tau_1 - \tau_2)$
- Thermal edge defined using deviation from std. div. in horizontal slice: $\phi'(x,y,z) > \sigma(\phi(z))$ (as in Couvreur et al 2010)

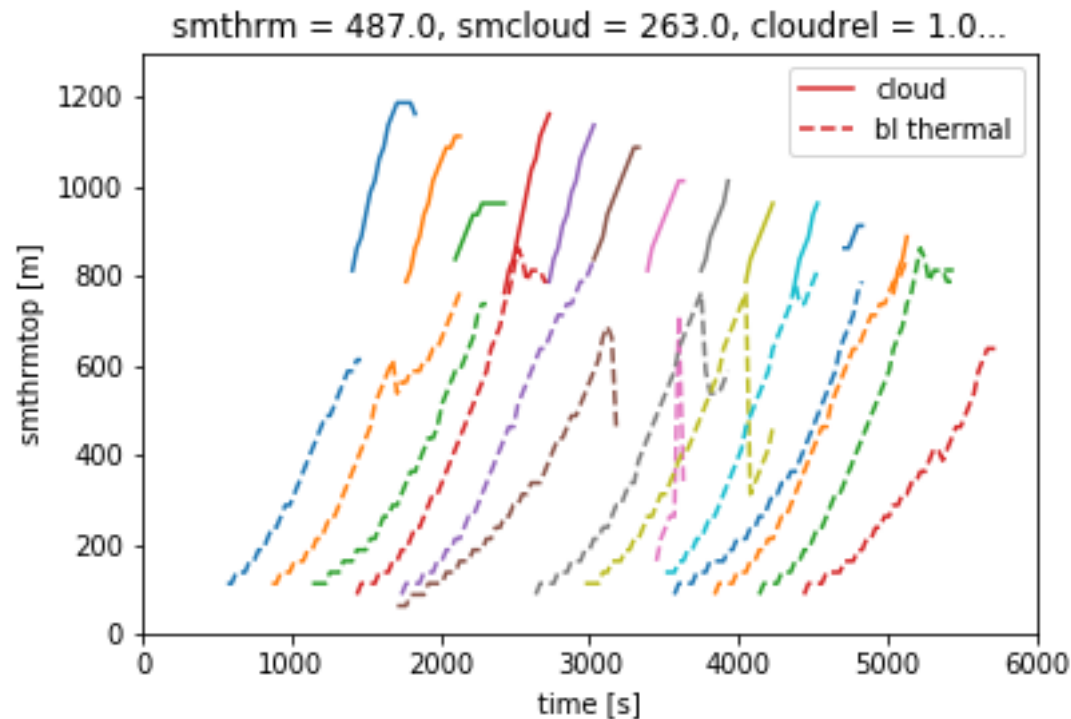
Radioactive tracer picks out air entering clouds



- We can now identify the air that enters clouds and look at its properties
- In this case the mean and distribution appears translated with height => should be easy to parameterise

(we can also track them...)

Updated cloud-tracking code by Heus 2008 to track thermals, and clouds, and interaction between them



Height of top of individual clouds and thermals that each cloud was triggered by

- Both thermals and clouds are tracked separately (using rad. tracer and liquid water)
- Can study properties of air triggering specific clouds
- Currently ~60% clouds have triggering thermals identified. Another trigger mechanism? Investigating cut-offs in tracking

...but that is part of object-based analysis, discussed later

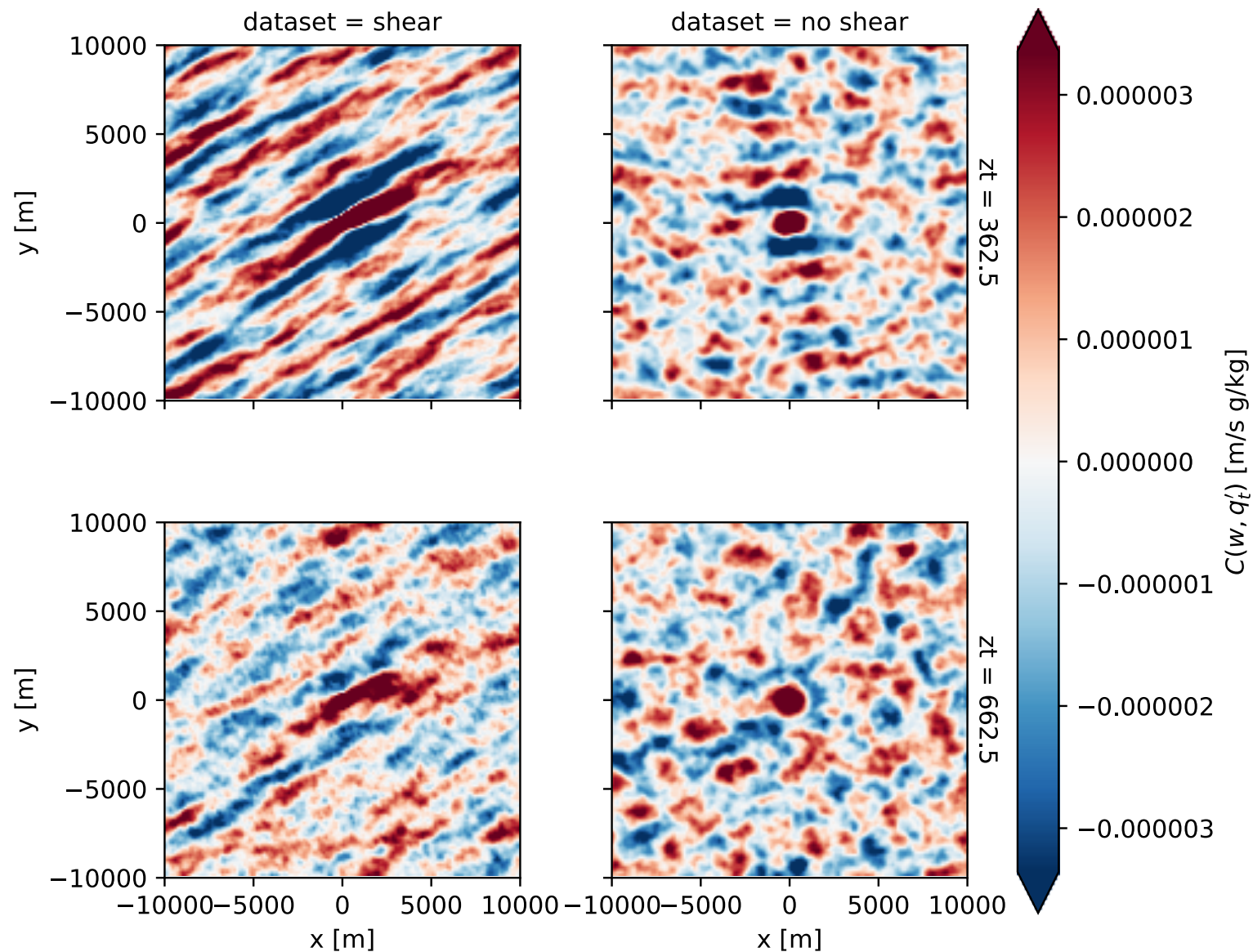
1.b. Characteristic length-scales of boundary-layer structures

- Two-point correlation of two scalar fields (ϕ and ψ), here taken at same height (z) for both fields

$$c_{\phi\psi}(\xi, \mu, z) = \frac{1}{L_x L_y} \int_0^{L_x} \int_0^{L_y} \phi'(x, y, z) \psi'(x + \xi, y + \mu, z) dx dy$$

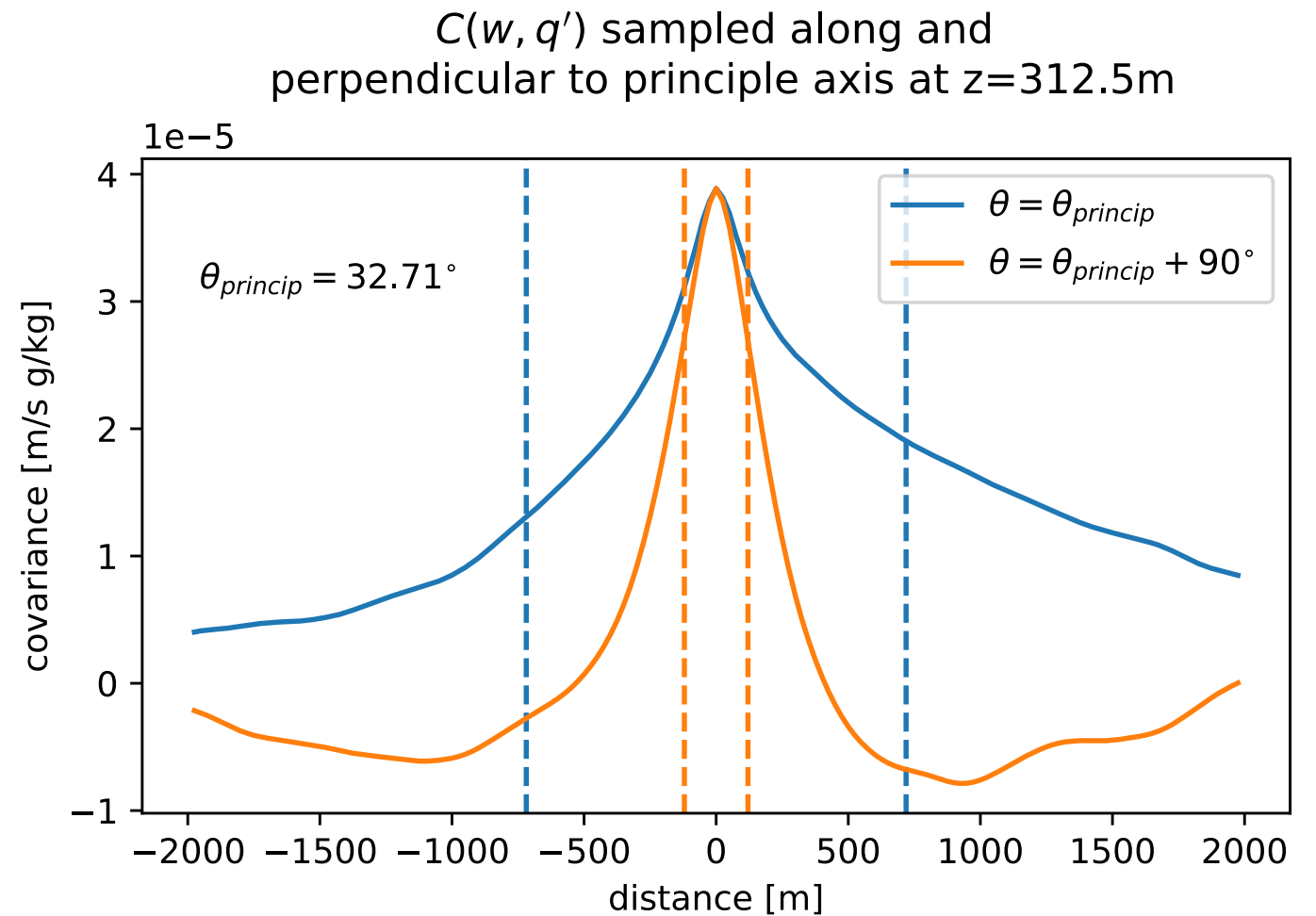
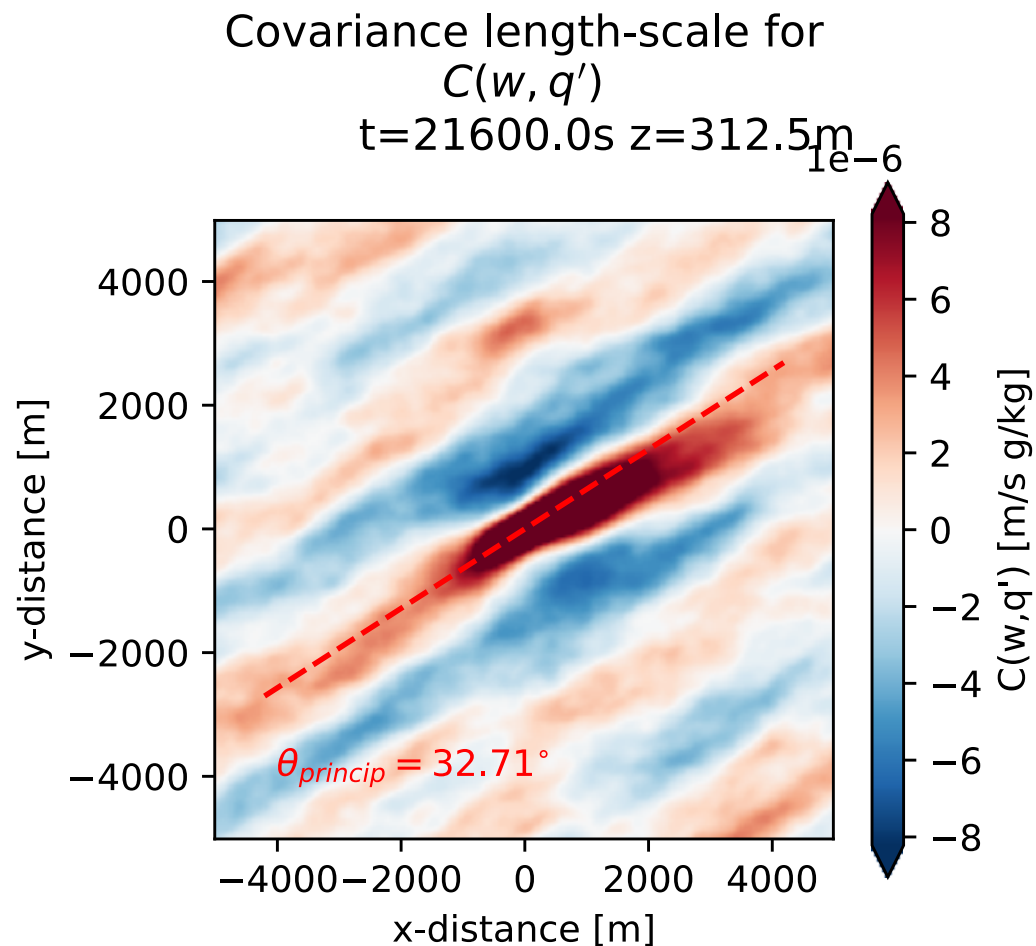
- Measures how correlation with distance (in xy -plane) of scalar fields
- Used by Tobias and Marston 2016 to identify principle length-scales diffusive transport in 3D Couette flow

Use of cumulants to study characteristic scales



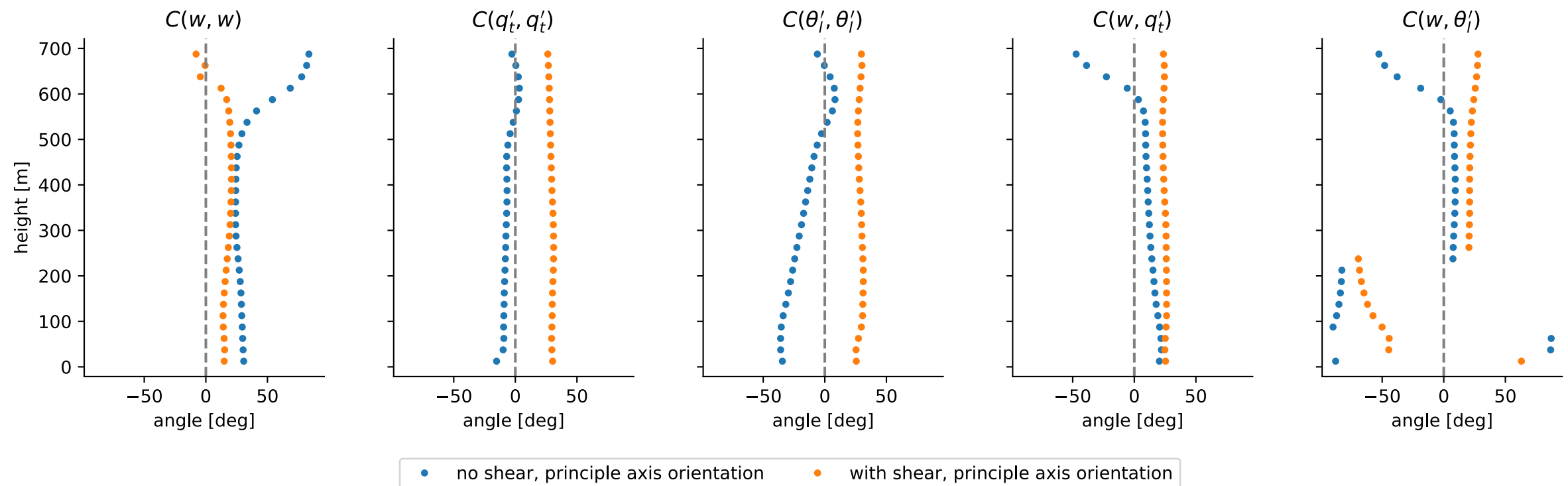
- With shear coherence is increased in direction of shear
 - Coherence stronger in mid boundary-layer than at cloud-base
- Non-sheared case *does* show coherence length-scale, characteristic scale of convective cells?
 - Similar scale to cross-shear coherence length-scale?

Use of cumulants to study characteristic scales



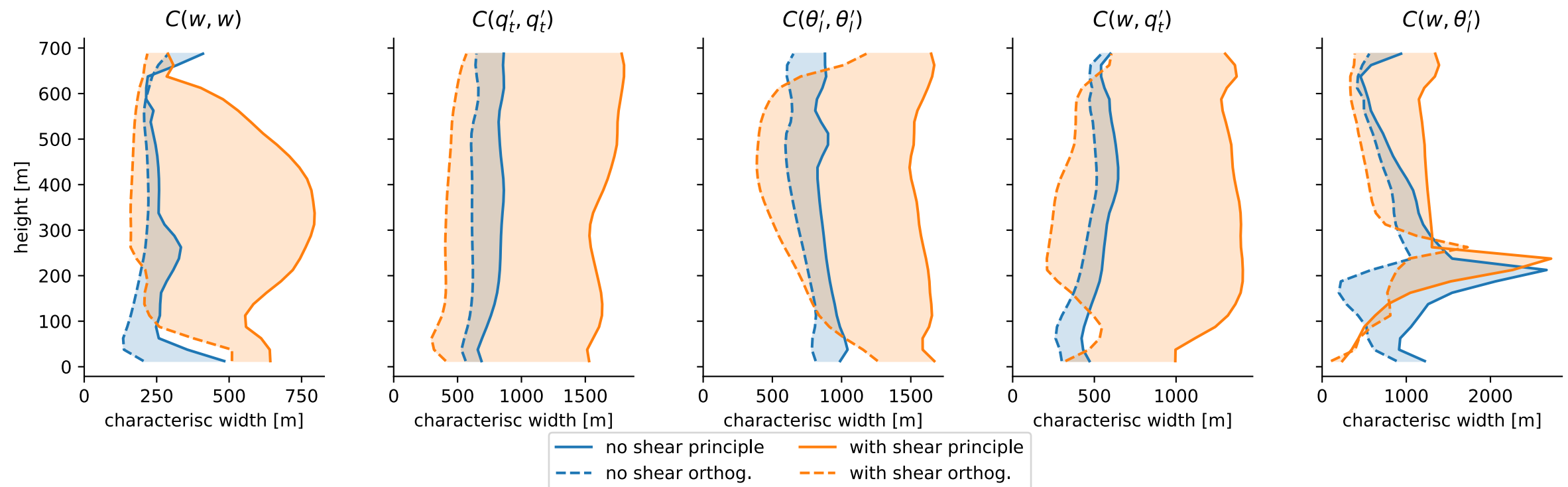
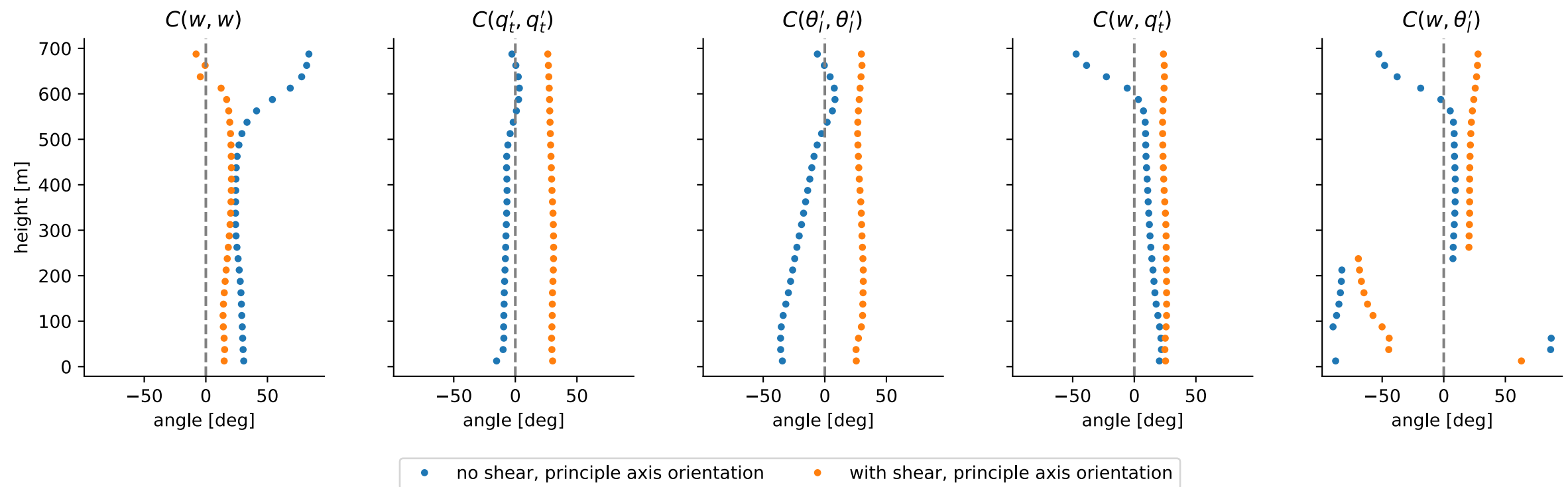
- Direction of strongest coherence from principle axis of moment of inertia tensor
- Coherence length-scale calculated as moment of covariance

Characteristic length-scales of vertical flux fields



- With shear all fields but heat-flux (θ_l) are oriented in same direction
 - Twist in vertical velocity angle at cloud-base?
- Without shear different fields have different orientation, but appears quite stable (smooth change) with height
- Heat-flux is small in simulation (over ocean => buoyancy from moisture flux, not heat flux), so probably little anisotropy

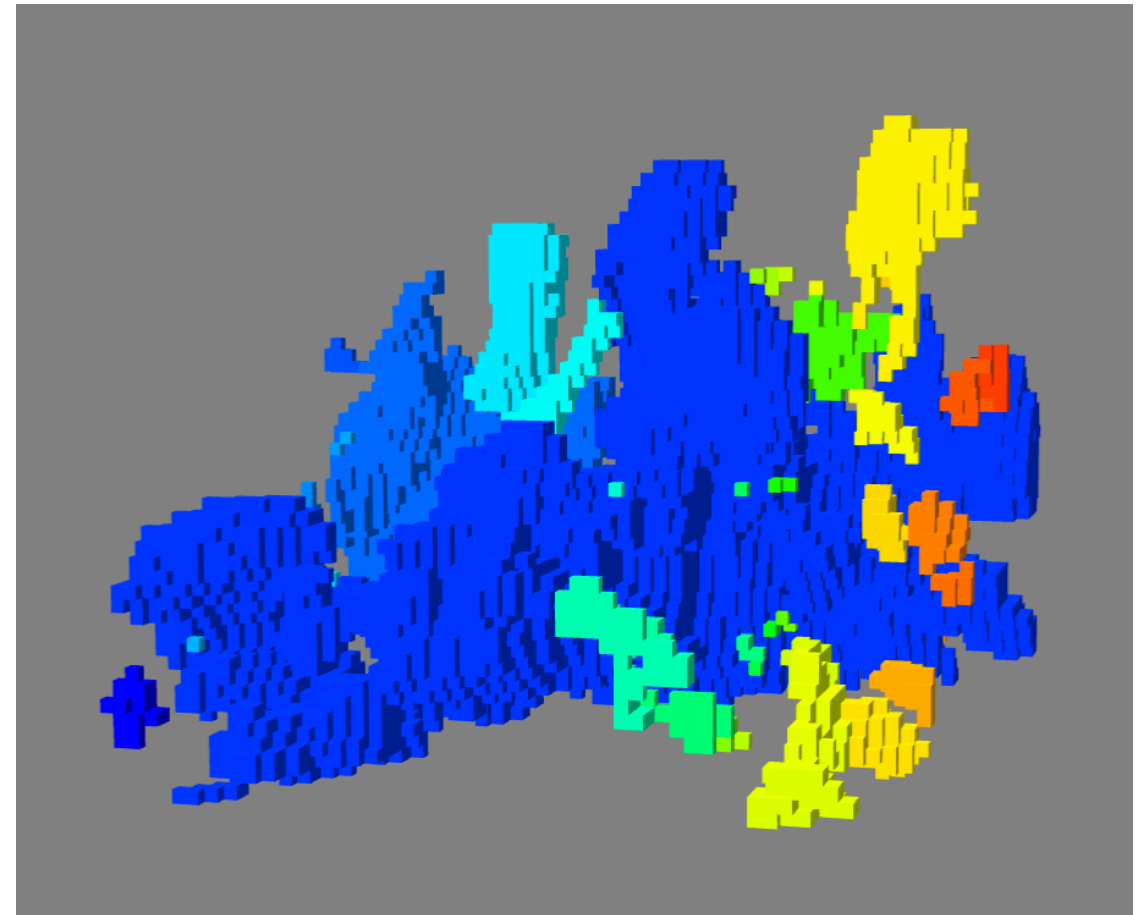
Characteristic length-scales of vertical flux fields



2. Object-based analysis

Identifying individual objects

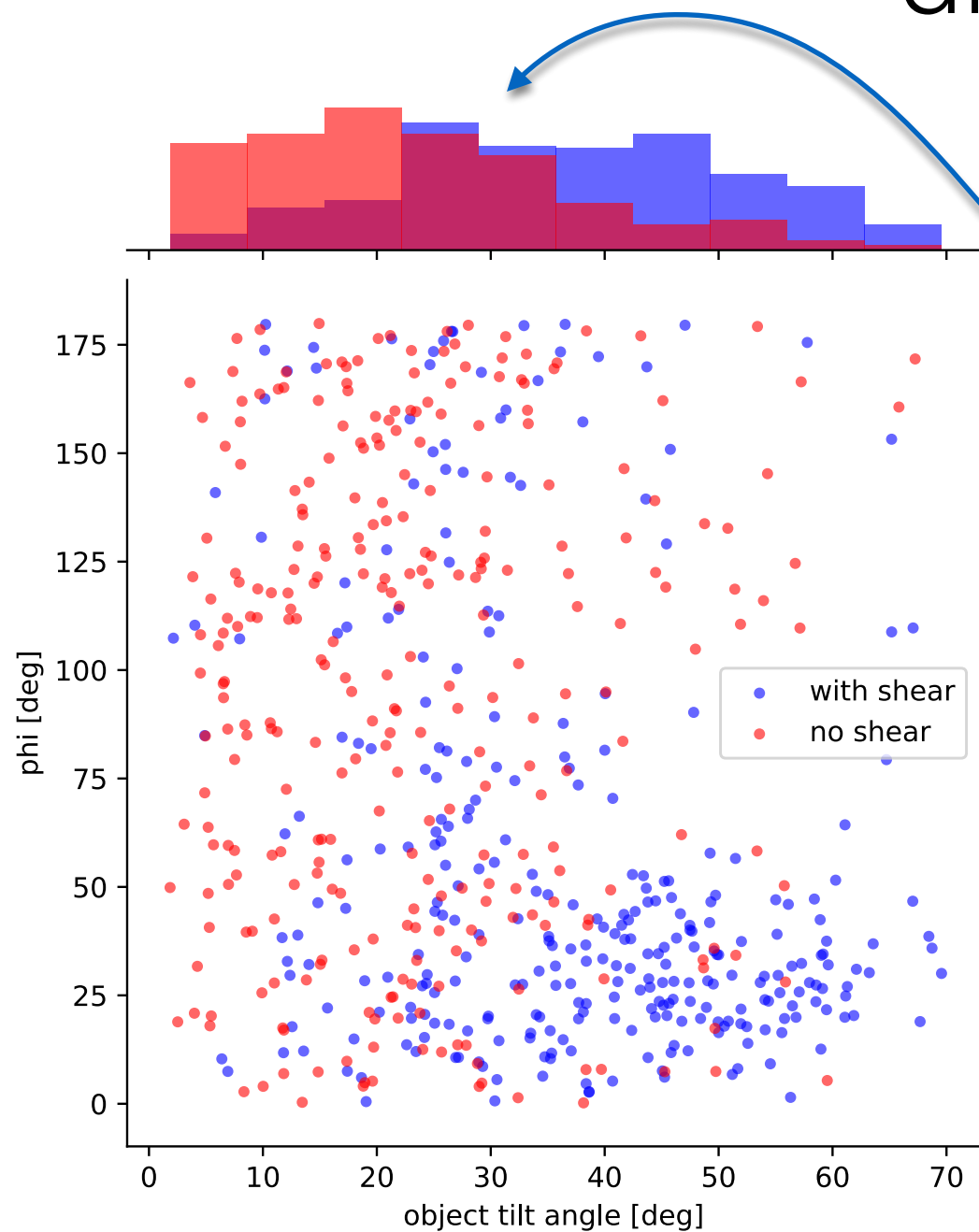
- Identify (and later, track in time) boundary layer structures which cause convection to trigger
- Use to partition distributions of variability by individual objects (of specific size, volume, shape, etc)



*Buoyant elements defined by $w > 0.5\text{m/s}$
in boundary layer of RICO simulation at $t=480\text{min}$*

- ➔ Investigating using object topology as means of classification. Contour-tree and fiber-surfaces analysis with Hamish Carr and PhD student, Leeds

Are the objects oriented with cumulant direction?



Yes! $\sim 30^\circ$

- Although objects in non-sheared environment appear titled no correlation with orientation
- Shear tilts objects in direction of shear

- Tilt and orientation calculate from slope of center-of-mass in every height inside object

What are characteristic sizes of objects in the boundary layer?

- Use Minkowski functionals to compute characteristic length-scales

$$\begin{aligned}
 V_0 &= V = \int dV \\
 V_1 &= \frac{A}{6} = \frac{1}{6} \int dS \\
 V_2 &= \frac{H}{3\pi} = -\frac{1}{6\pi} \int dS \nabla \cdot \hat{n} \\
 \left(V_3 &= \frac{1}{4\pi} \int (\kappa_1 \kappa_2) dS \right)
 \end{aligned}
 \quad \Rightarrow \quad
 \begin{aligned}
 L &= \frac{3V_2}{4V_3} \\
 W &= \frac{2V_1}{\pi V_2} \\
 T &= \frac{V_0}{2V_1}
 \end{aligned}$$

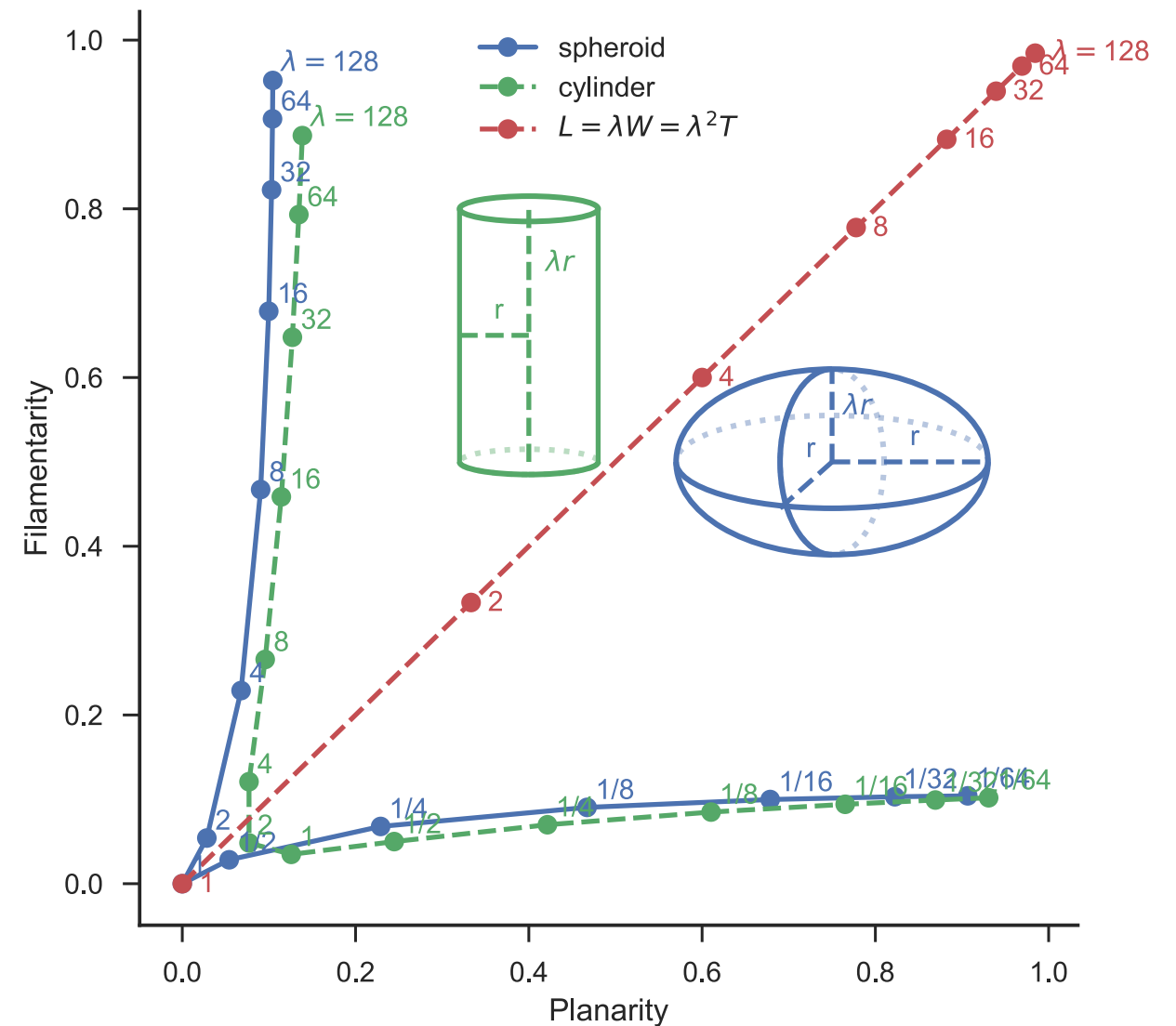
$L \geq W \geq T$ by construction

V: volume, A: area, H: mean curvature, κ_1 and κ_2 intrinsic local curvature ($\nabla \cdot \hat{n} = \kappa_1 + \kappa_2$)

What is shape of objects in the boundary layer?

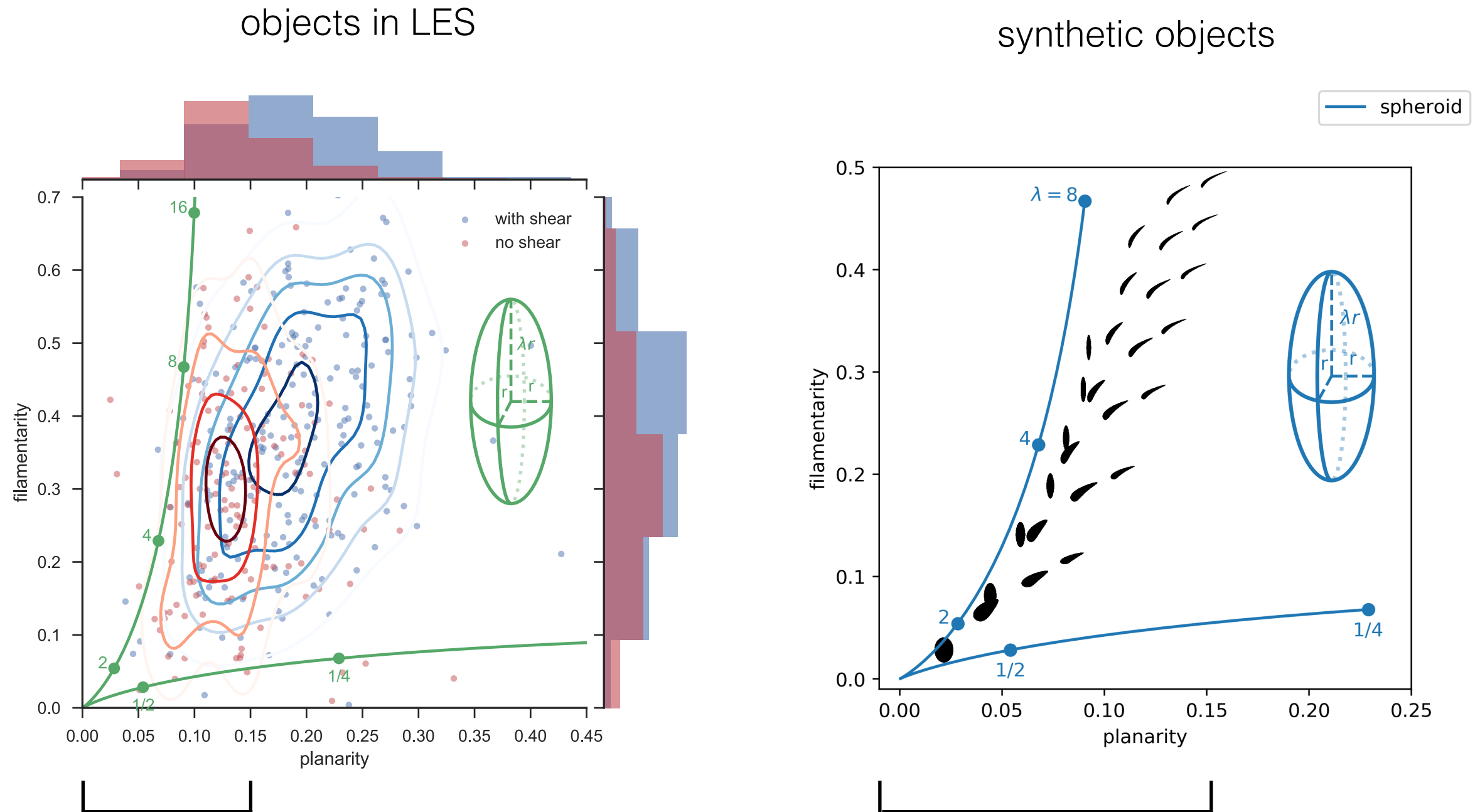
Calculate the planarity (P) and filamentary (F) from Minkowski functional length-scales

$$P = \frac{W - T}{W + T}, F = \frac{L - W}{L + W}$$



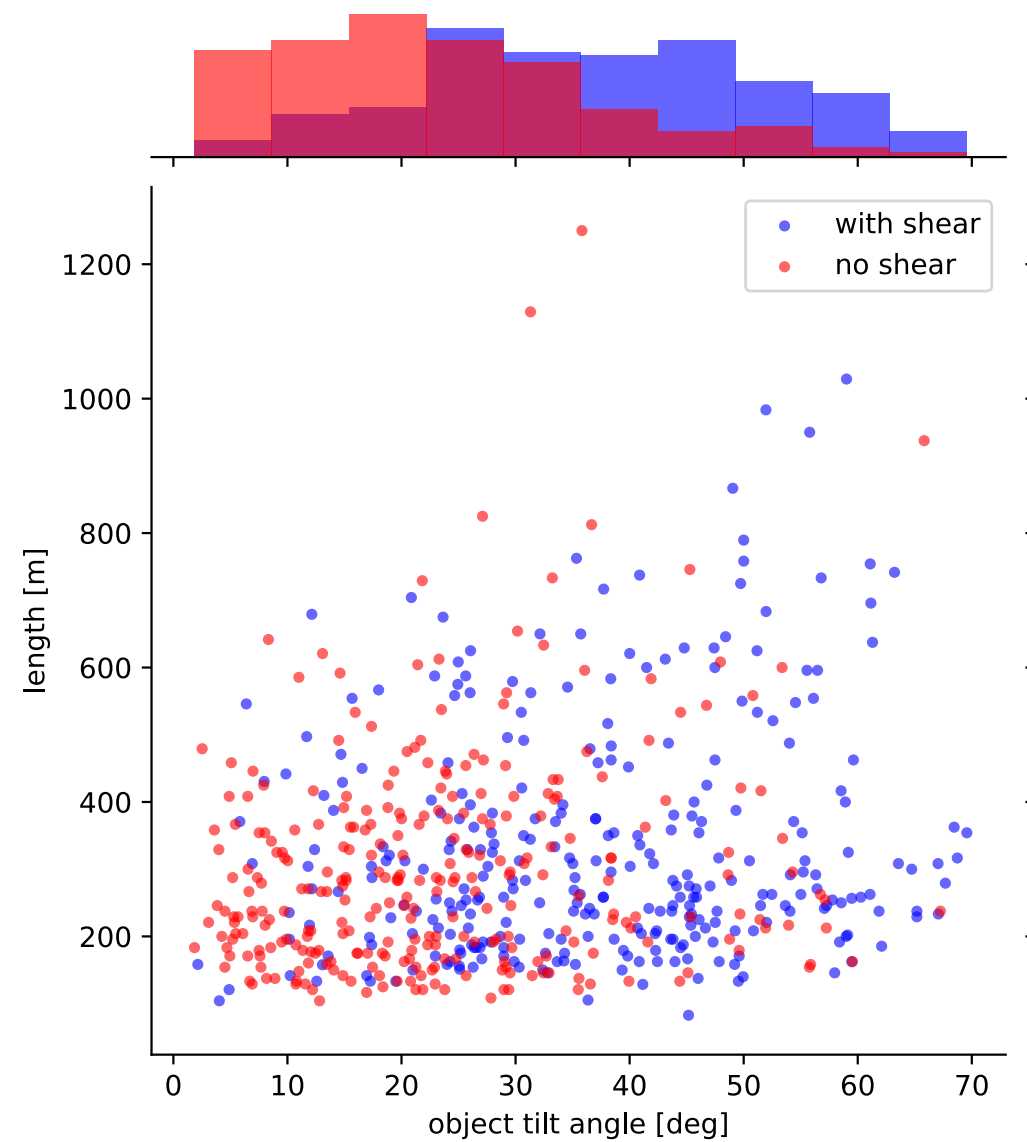
➔ Measures how pencil or disc-like an object is

What is shape of objects in the boundary layer?



- ➔ Shear causes structures to become longer and wider by $\sim 30\%$ and $\sim 50\%$ respectively

Does object tilt correlate with length?



- ➔ Doesn't appear to be a large effect, but maybe obscured by large number of small objects

Next steps

Papers being written

1. Demonstration of cumulants and Minkowski functionals as means to quantify bulk and object-based properties of atmospheric fluids with coherent structures
2. Investigation of the effect of changing Bowen-ratio on properties coherent structures in the boundary layer

Ongoing work:

- I. Developing topography test-case to do parameter study (bulk surface moisture flux and topography height)
- II. Setting up/finding cases with deeper convection and diurnal cycle
- III. Developing predictive model for properties of boundary-layer coherent structures

Thank you!

Questions?