

Supplementary information

Gladstone-Dale relationship

Equation 1 The Gladstone-Dale relationship between the refractive energy K ; refractive index n ; density ρ of a mineral and its respective constituents. Where k_1, k_2 and w_1, w_2 represent the constituent refractive energies and weight ratios respectively.

$$K = \frac{(n - 1)}{\rho} = k_1 w_1 + k_2 w_2 + \dots k_n w_n \quad (2)$$

Particle settling under centrifugation

Particle settling in centrifugal field is acted upon by two opposing forces, a centrifugal force and a drag force. Under laminar flow conditions (small particle sizes):

Inertial centrifugal force acting on a spherical particle:

$$F_{IC} = m\omega^2 R = \frac{4}{3}\pi r^3 \rho_{particle} \omega^2 R$$

Buoyancy force acting on particle, where α is angular acceleration:

$$F_B = \frac{4}{3}\pi r^3 \rho_{fluid} \alpha = \frac{4}{3}\pi r^3 \rho_{fluid} \omega^2 R$$

Viscous drag force acting on particle:

$$F_D = 6\pi r \mu V$$

Relative centrifugal force:

$$RCF = \frac{\omega^2 R}{g}$$

Force balance acting on a spherical particle at terminal velocity falling through a viscous fluid:

$$F_{IC} = F_B + F_D$$
$$\frac{4}{3}\pi r^3 \rho_{particle} \omega^2 R - \frac{4}{3}\pi r^3 \rho_{fluid} \omega^2 R = 6\pi r \mu V$$

$$\frac{2 r^2 \Delta \rho \omega^2 R}{9 \mu} = V_s$$

$$\boxed{\frac{2 r^2 \Delta \rho \omega^2 R}{9 \mu} = t_s}$$

Where:

$\rho_{particle}$ = particle density

ρ_{fluid} = fluid density

$\omega = \text{angular velocity}$

$\alpha = \text{angular acceleration} = \omega^2 R$

$R = \text{radius of centrifugation}$

$r = \text{spherical particle radius}$

$V_s = \text{terminal particle velocity}$

$t_s = \text{terminal particle settling time}$

For a centrifugation time of 3minutes (180s), supernatant travel distance of 2cm; a graph may be constructed (Figure 1) to approximate terminal particle settling time:

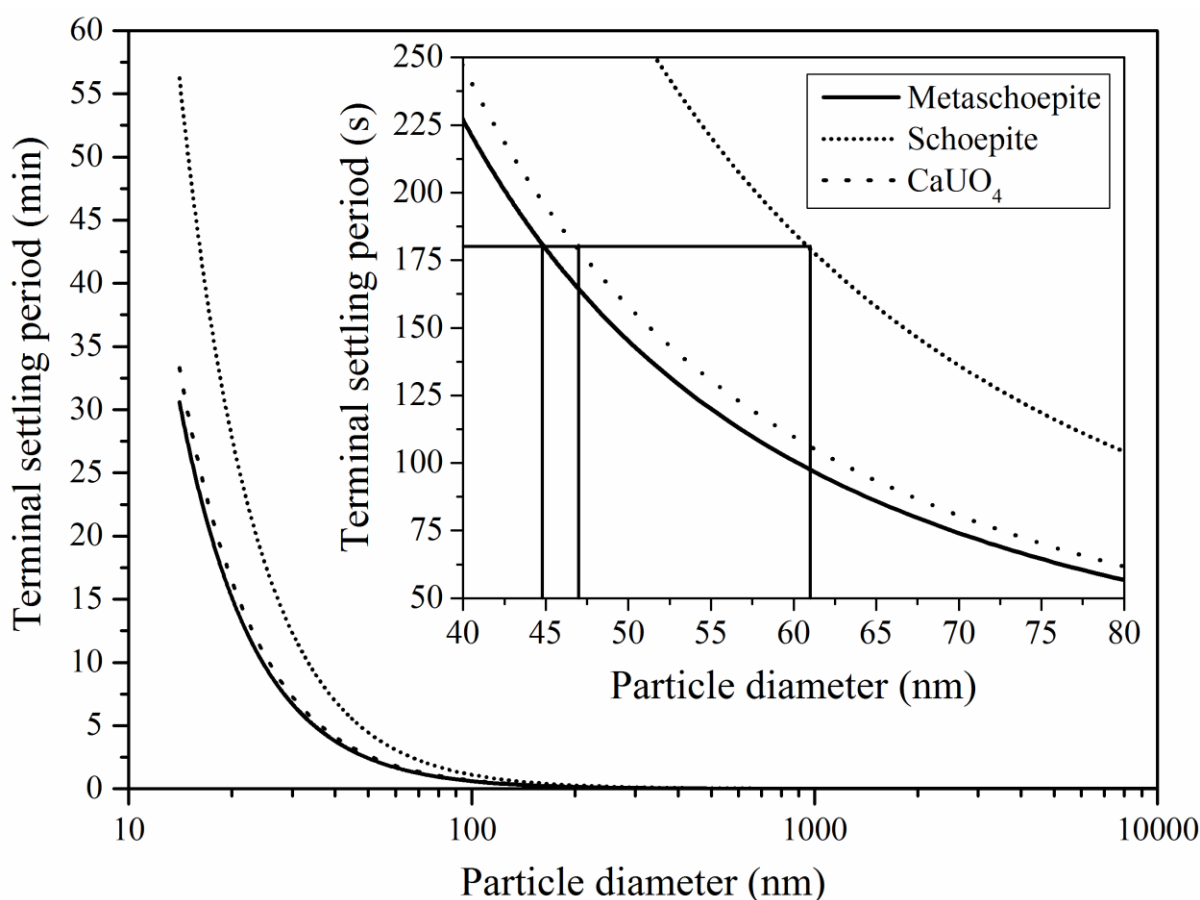
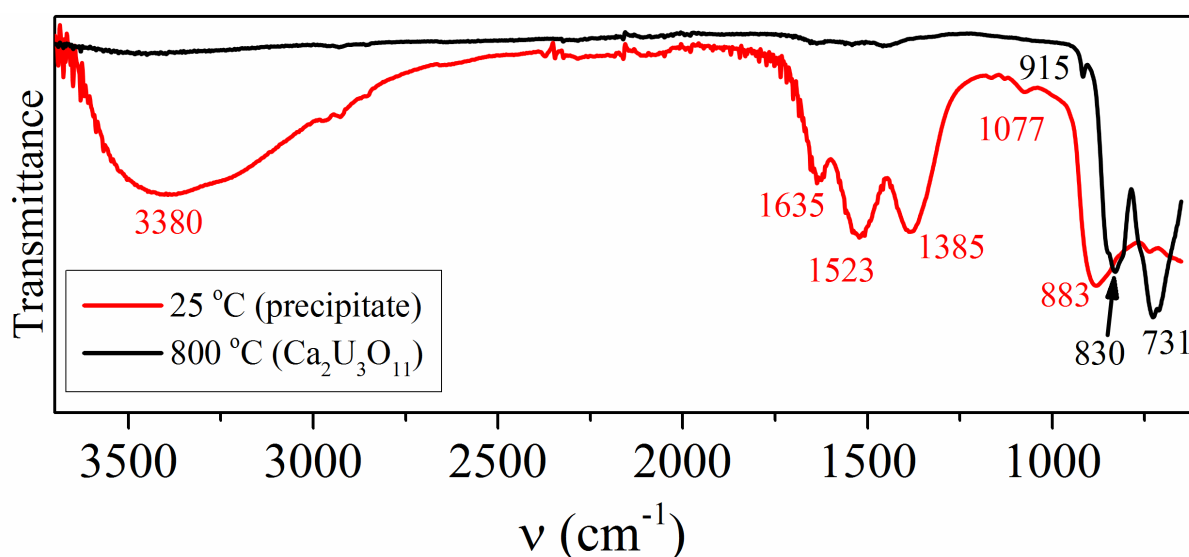


Figure 1 Graph of predicted nanometric spherical particles settling times. (Water at 25°C $\mu = 0.89 \text{ mN s m}^{-2}$ [1]); ρ_p is particle density (Schoepite: ICSD 82477, $\rho = 4818.64 \text{ kg m}^{-3}$, Metaschoepite: ICSD 23647, $\rho = 8017.66 \text{ kg m}^{-3}$, CaUO₄: ICSD 31631, $\rho = 7450 \text{ kg m}^{-3}$); ρ_f is fluid density (Water at 25°C, $\rho = 997.1 \text{ kg m}^{-3}$ [1]); R is 0.06m.

Fourier Transform Infra-Red (FTIR) spectroscopy

Powdered samples (~20mg) were analysed using an A2 Microlab Portable mid-IR spectrometer with a Diamond Internal reflection cell (DATR). 10 measurements were completed for each sample and merged.



Na ₂ U ₂ O ₇ ·6H ₂ O [2]	Literature data			This study		Assignment
	Becquerelite [3]	CaU ₂ O ₇ [4]	Ba ₂ U ₃ O ₁₁ [4]	25 °C	800 °C	
3379-3578	3504			2500-3700		ν H ₂ O, OH
1645	1625			1635		δ H ₂ O
	1250			1385-1523		ν ₃ NO ₃
	997			1077		δ UOH in-plane
936	927					
882	840			883		ν ₃ UO ₂ ²⁺
	812					
		835	830		830	U=O
		730	750		731	U-O

Figure 2 FTIR spectra of poorly crystalline hydrous Ca-uranate (25 °C) formed at pH 12 and crystalline Ca-uranate (Ca₂U₃O₁₁) after dehydration at 800 °C with summarised tentative band assignments based on literature data for analogous compounds.

Summary of derived molar [Ca/U] stoichiometry and formulae from analyses

Method	Molar [Ca/U] ratio	Stoichiometric formula
SEM-EDS	0.63 ± 0.02	Ca ₂ U _{3.18} O _{11.5}
pXRD-Rietveld	0.60 ± 0.03	Ca ₂ U _{3.32} O ₁₂
ICP-OES	0.68 ± 0.04	Ca ₂ U _{2.92} O _{10.77}
		(I) Ca ₂ (UO ₂) ₃ O _{3.75} (OH) _{2.5} ·3.5H ₂ O
		(II) Ca ₂ (UO ₂) ₃ O _{3.75} (OH) _{2.5}
TG	-	(III) Ca ₂ U ₃ O ₁₁
		(IV) CaUO ₄ , UO ₂
Average	0.64 ± 0.03	Ca ₂ U _{3.1} O _{11.4}

1. Kestin, J., M. Sokolov, and W.A. Wakeham, *Viscosity of liquid water in the range– 8 C to 150 C*. Journal of Physical and Chemical Reference Data, 1978. **7**(3): p. 941-948.
2. Chernorukov, N.G., O.V. Nipruk, and E.L. Kostrova, *Synthesis and study of sodium uranate Na₂U₂O₇·6H₂O and of products of its dehydration and thermal decomposition*. Radiochemistry, 2016. **58**(2): p. 124-127.
3. Cejka, J., *Infrared spectroscopy and thermal analysis of the uranyl minerals*. Reviews in Mineralogy and Geochemistry, 1999. **38**(1): p. 521-622.

4. Allen, G.C. and A.J. Griffiths, *Vibrational spectroscopy of alkaline-earth metal uranate compounds*. Journal of the Chemical Society, Dalton Transactions, 1979(2): p. 315-319.